

# Cambridge IGCSE<sup>™</sup>

CANDIDATE NAME		
CENTRE NUMBER		CANDIDATE NUMBER
ADDITIONAL MATHEMATICS 06		0606/21
Paper 2		October/November 2020
		2 hours

You must answer on the question paper.

No additional materials are needed.

#### INSTRUCTIONS

- Answer **all** questions.
- Use a black or dark blue pen. You may use an HB pencil for any diagrams or graphs.
- Write your name, centre number and candidate number in the boxes at the top of the page.
- Write your answer to each question in the space provided.
- Do **not** use an erasable pen or correction fluid.
- Do **not** write on any bar codes.
- You should use a calculator where appropriate.
- You must show all necessary working clearly; no marks will be given for unsupported answers from a calculator.

This document has **16** pages. Blank pages are indicated.

• Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place for angles in degrees, unless a different level of accuracy is specified in the question.

#### INFORMATION

- The total mark for this paper is 80.
- The number of marks for each question or part question is shown in brackets [].

[Turn over

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### Mathematical Formulae

#### 1. ALGEBRA

Quadratic Equation

For the equation  $ax^2 + bx + c = 0$ ,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

**Binomial Theorem** 

$$(a+b)^{n} = a^{n} + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^{2} + \dots + \binom{n}{r}a^{n-r}b^{r} + \dots + b^{n}$$

1)d

where *n* is a positive integer and  $\binom{n}{r} = \frac{n!}{(n-r)!r!}$ 

Arithmetic series 
$$u_n = a + (n-1)d$$
  
 $S_n = \frac{1}{2}n(a+l) = \frac{1}{2}n\{2a+(n-1)d\}$ 

*Geometric series* 

$$u_n = ar^{n-1}$$

$$S_n = \frac{a(1-r^n)}{1-r} \quad (r \neq 1)$$

$$S_{\infty} = \frac{a}{1-r} \quad (|r| < 1)$$

## 2. TRIGONOMETRY

Identities

$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$
$$\csc^2 A = 1 + \cot^2 A$$

Formulae for  $\triangle ABC$ 

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
$$a^{2} = b^{2} + c^{2} - 2bc \cos A$$
$$\Delta = \frac{1}{2}bc \sin A$$

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1 Solve the inequality |3x+2| > 8+x.

2 Find the coordinates of the points of intersection of the curve  $x^2 + xy = 9$  and the line  $y = \frac{2}{3}x - 2$ . [5]

Write  $3 \lg x + 2 - \lg y$  as a single logarithm. 3

- It is given that  $y = \ln(\sin x + 3\cos x)$  for  $0 < x < \frac{\pi}{2}$ . (a) Find  $\frac{dy}{dx}$ . 4

[3]

[3]

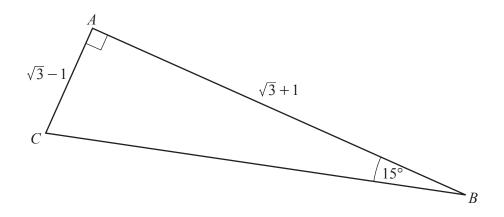
**(b)** Find the value of x for which  $\frac{dy}{dx} = -\frac{1}{2}$ . [3]

https://xtremepape.rs/

5 The first three terms in the expansion of  $(a+bx)^5(1+x)$  are  $32-208x+cx^2$ . Find the value of each of the integers *a*, *b* and *c*. [7]

# 6 DO NOT USE A CALCULATOR IN THIS QUESTION.

In this question all lengths are in centimetres.



In the diagram above  $AC = \sqrt{3} - 1$ ,  $AB = \sqrt{3} + 1$ , angle  $ABC = 15^{\circ}$  and angle  $CAB = 90^{\circ}$ .

(a) Show that 
$$\tan 15^\circ = 2 - \sqrt{3}$$
. [3]

(b) Find the exact length of *BC*.

[2]

# 7 DO NOT USE A CALCULATOR IN THIS QUESTION.

$$p(x) = 2x^3 - 3x^2 - 23x + 12$$
  
(a) Find the value of  $p(\frac{1}{2})$ . [1]

(b) Write p(x) as the product of three linear factors and hence solve p(x) = 0. [5]

- 8 The population *P*, in millions, of a country is given by  $P = A \times b^t$ , where *t* is the number of years after January 2000 and *A* and *b* are constants. In January 2010 the population was 40 million and had increased to 45 million by January 2013.
  - (a) Show that b = 1.04 to 2 decimal places and find A to the nearest integer. [4]

(b) Find the population in January 2020, giving your answer to the nearest million. [1]

(c) In January of which year will the population be over 100 million for the first time? [3]

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- 9 A particle moves in a straight line such that, t seconds after passing a fixed point O, its displacement from O is s m, where  $s = e^{2t} 10e^t 12t + 9$ .
  - (a) Find expressions for the velocity and acceleration at time *t*. [3]

(b) Find the time when the particle is instantaneously at rest.

(c) Find the acceleration at this time.

[2]

[3]

- 10 The gradient of the normal to a curve at the point (x, y) is given by  $\frac{x}{x+1}$ .
  - (a) Given that the curve passes through the point (1, 4), show that its equation is  $y = 5 \ln x x$ . [5]

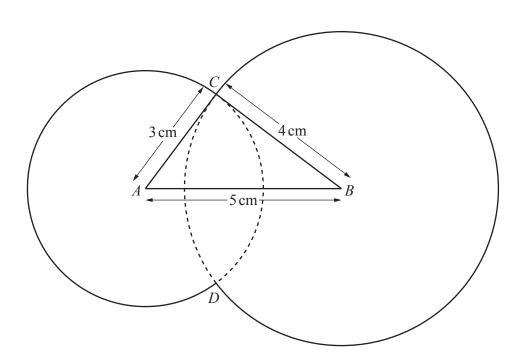
(b) Find, in the form y = mx + c, the equation of the tangent to the curve at the point where x = 3. [3]

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- 11 The equation of a curve is  $y = x\sqrt{16-x^2}$  for  $0 \le x \le 4$ .
  - (a) Find the exact coordinates of the stationary point of the curve.

[6]

(b) Find  $\frac{d}{dx}(16-x^2)^{\frac{3}{2}}$  and hence evaluate the area enclosed by the curve  $y = x\sqrt{16-x^2}$  and the lines y = 0, x = 1 and x = 3. [5]



The diagram shows a shape consisting of two circles of radius 3 cm and 4 cm with centres A and B which are 5 cm apart. The circles intersect at C and D as shown. The lines AC and BC are tangents to the circles, centres B and A respectively. Find

(a) the angle *CAB* in radians,

[2]

(b) the perimeter of the whole shape,

(c) the area of the whole shape.

[4]

[4]

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